



Algebra 2 – Year 2

Name: _____

Review Sheet #1: Lessons 11.1-11.2, 11.8 Date: _____ Hour: _____

Show the set up for ALL problems!

For problems 1–3, find the probability of each event as a simplified fraction and a percent, to the nearest tenth.

1. A box contains 6 green, 5 yellow, and 3 purple balls. Find the probability of drawing a green ball in a single random draw. 1. _____ FRACTION PERCENT

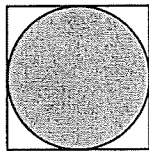
2. When a number cube is rolled, a number less than 5 appears. 2. _____ FRACTION PERCENT

3. A card is chosen at random from a standard deck is a king, or ace. 3. _____ FRACTION PERCENT

4. Find the number of possible passwords for 3 letters followed by 3 digits, with only consonants (consider “y” a consonant) and odd digits allowed. 4. _____

5. An ice cream shop has 21 flavors of ice cream, 7 toppings, and 8 mix-ins. How many different sundaes can the shop make? 5. _____

6. If one point is randomly selected from the points inside the rectangle shown below, find the probability that the point is in the circle. (Remember: Area of a circle = πr^2) 6. _____



12cm

For problems 7-15, evaluate each expression. (Show all work - Only use your calculator to multiply or divide.) (1.5 pts each)

7. $\frac{10!}{4! \times 6!}$ 8. ${}_9P_3$ 7. _____

8. _____

9. ${}_7C_3$

10. $\frac{(7-3)! \times 3!}{2! \times 0!}$

9. _____

10. _____

11. Ten people buy tickets for a raffle. 1st place wins \$100, 2nd place wins \$50, and 3rd place wins \$10. How many different arrangements of 1st, 2nd, and 3rd place winners are possible?

11. _____

12. In how many ways can 3 singers be selected from 5 who came to an audition?

12. _____



13. How many ways can 4 DVDs be borrowed from a collection of 25 DVDs?

13. _____

14. How many ways can 10 horses line up for a race?

14. _____

Expand the binomial raised to a power.

15. $(x+2y)^4$



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Review Sheet #1: Lessons 11.1-11.2, 11.8 Date: _____ Hour: _____

Show the set up for ALL problems!

For problems 1-3, find the probability of each event as a simplified fraction and a percent, to the nearest tenth.

1. A box contains 6 green, 5 yellow, and 3 purple balls. Find the probability of drawing a green ball in a single random draw. $6+5+3=14$

$$P(\text{green}) = \frac{6}{14} = \frac{3}{7} = 0.429 \rightarrow 42.9\%$$

1. $\frac{3}{7}$ 42.9%
 FRACTION PERCENT

2. When a number cube is rolled, a number less than 5 appears.

1 2 3 4 5 6 $P(<5) = \frac{4}{6} = \frac{2}{3} = 0.667 \rightarrow 66.7\%$

2. $\frac{2}{3}$ 66.7%
 FRACTION PERCENT

3. A card is chosen at random from a standard deck is a king, or ace.

Total 52 cards
 4 kings & 4 aces $P(\text{king or ace}) = \frac{4+4}{52} = \frac{8}{52} = \frac{2}{13} = 0.154$

3. $\frac{2}{13}$ 15.4%
 FRACTION PERCENT

4. Find the number of possible passwords for 3 letters followed by 3 digits, with only consonants (consider "y" a consonant) and odd digits allowed.

26
~~5 vowels~~
 21 consonants 1, 3, 5, 7, 9 = 5 odd digits
 $21 \cdot 21 \cdot 21 \cdot 5 \cdot 5 \cdot 5 = 1,157,625$

4. _____

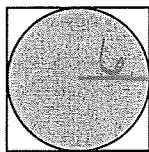
5. An ice cream shop has 21 flavors of ice cream, 7 toppings, and 8 mix-ins. How many different sundaes can the shop make?

$$21 \cdot 7 \cdot 8 = 1176$$

5. _____

6. If one point is randomly selected from the points inside the rectangle shown below, find the probability that the point is in the circle.

(Remember: Area of a circle = πr^2)



12cm

$r = 6$ Area(circle) = $\pi(6)^2$
 $= 36\pi$

Total area = $12^2 = 144$

$P(\text{circle}) = \frac{36\pi}{144} = 0.785 \rightarrow 78.5\%$

6. _____

For problems 7-15, evaluate each expression. (Show all work - Only use your calculator to multiply or divide.) (1.5 pts each)

7. $\frac{10!}{4! \times 6!} = 210$

8. ${}_9P_3 = \frac{9!}{(9-3)!}$

7. _____

$= 504$

8. _____

$$9. {}_7C_3 = \frac{7!}{(7-3)!3!}$$

$$= 35$$

$$10. \frac{(7-3)! \times 3!}{2! \times 0!}$$

$$\frac{4!3!}{2!} = 72$$

9. _____

10. _____

11. Ten people buy tickets for a raffle. 1st place wins \$100, 2nd place wins \$50, and 3rd place wins \$10. How many different arrangements of 1st, 2nd, and 3rd place winners are possible?

11. _____

Order Matters! Permutation

$${}_{10}P_3 = \frac{10!}{(10-3)!} = 720$$

12. In how many ways can 3 singers be selected from 5 who came to an audition?

12. _____

Order Does NOT matter! Combination

$${}_{5}C_3 = \frac{5!}{(5-3)!3!} = 10$$

13. How many ways can 4 DVDs be borrowed from a collection of 25 DVDs?

13. _____

Order does not matter! Combination

$${}_{25}C_4 = \frac{25!}{(25-4)!4!} = 12650$$

14. How many ways can 10 horses line up for a race?

14. _____

$$10 \cdot 9 \cdot 8 \cdot \dots \cdot 1 = 10!$$

$$= 3,628,800$$

Expand the binomial raised to a power.

$$15. (x+2y)^4$$

$$\binom{4}{0}x^4(2y)^0 + \binom{4}{1}x^3(2y)^1 + \binom{4}{2}x^2(2y)^2 + \binom{4}{3}x^1(2y)^3 + \binom{4}{4}x^0(2y)^4$$

$$\rightarrow 1 \cdot x^4 \cdot 1 + 4 \cdot x^3 \cdot 2y + 6 \cdot x^2 \cdot 4y^2 + 4 \cdot x \cdot 8y^3 + 1 \cdot 1 \cdot 16y^4$$

$$x^4 + 8x^3y + 24x^2y^2 + 32xy^3 + 16y^4$$

${}_{4}C_0$



Lesson 11.1 – Permutations & Combinations

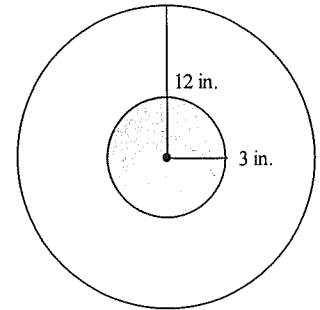
1. In how many different orders can you line up 8 cards on a table?
2. In how many ways can 12 basketball players be listed in a program?
3. Suppose Ruth Ann has 3 routes she can choose from to get from school to the library, and 5 routes from the library to her home. How many routes are there from Ruth Ann's school to her home with a stop at the library?
4. A yogurt shop offers 6 different flavors of frozen yogurt and 12 different toppings. How many choices are possible for a single serving of frozen yogurt with one topping?
5. At a deli, a sub sandwich can be ordered with any of 7 different condiments. In how many different ways can a sandwich with exactly 3 condiments be ordered?
6. Evaluate ${}_9P_4$.
7. Evaluate $\frac{{}_{60}C_3}{{}_{15}C_3}$.
8. Evaluate ${}_7C_6$.
9. Eight teams enter a tournament. How many arrangements of 1st, 2nd, and 3rd place winners are possible?

Lesson 11.2 - Probability

10. Lynn and Dawn tossed a coin 60 times and got heads 33 times. What is the experimental probability of tossing heads using Lynn and Dawn's results?
11. A bag contains 6 red marbles, 6 white marbles, and 4 blue marbles. Find $P(\text{red or blue})$.

12. A spinner is numbered from 1 through 10 with each number equally likely to occur. What is the probability of obtaining a number less than 2 in a single spin?

13. If a dart hits the target at random, what is the probability that it will land in the shaded region? (Remember: Area of a circle = πr^2)



Drawing not to scale

Lesson 11.8 – Binomial Theorem

Use the **Binomial Theorem** to find the binomial expansion of the expression.

14. $(a + b)^6$

Simplified answer: _____

15. $(c - 3)^4$

Simplified answer: _____



Lesson 11.1 – Permutations & Combinations

1. In how many different orders can you line up 8 cards on a table?

$$8 \cdot 7 \cdot 6 \cdot 5 \cdot 4 \cdot \dots \cdot 1 = 8! = 40320$$

2. In how many ways can 12 basketball players be listed in a program?

$$12 \cdot 11 \cdot 10 \cdot \dots \cdot 1 = 12! = 479001600$$

3. Suppose Ruth Ann has 3 routes she can choose from to get from school to the library, and 5 routes from the library to her home. How many routes are there from Ruth Ann's school to her home with a stop at the library?

$$3 \cdot 5 = 15$$

4. A yogurt shop offers 6 different flavors of frozen yogurt and 12 different toppings. How many choices are possible for a single serving of frozen yogurt with one topping?

$$6 \cdot 12 = 72$$

5. At a deli, a sub sandwich can be ordered with any of 7 different condiments. In how many different ways can a sandwich with exactly 3 condiments be ordered? *Order Does NOT matter!*

Combination

$${}^7C_3 = \frac{7!}{(7-3)!3!} = 35$$

6. Evaluate 9P_4 .

$$= \frac{9!}{(9-4)!} = 3024$$

7. Evaluate $\frac{{}^{60}C_3}{{}^{15}C_3}$.

$$= \frac{6844}{91} = 75.21$$

8. Evaluate 7C_6 .

$$= \frac{7!}{(7-6)!6!} = 7$$

9. Eight teams enter a tournament. How many arrangements of 1st, 2nd, and 3rd place winners are possible?

Order matters! Permutation

$${}^8P_3 = \frac{8!}{(8-3)!} = 336$$

Lesson 11.2 - Probability

10. Lynn and Dawn tossed a coin 60 times and got heads 33 times. What is the experimental probability of tossing heads using Lynn and Dawn's results?

$$P(\text{heads}) = \frac{33}{60} = \frac{11}{20} = 0.55 \rightarrow 55\%$$

11. A bag contains 6 red marbles, 6 white marbles, and 4 blue marbles. Find $P(\text{red or blue})$.

$$\text{Total marbles} = 16$$

$$P(\text{red or blue}) = \frac{6+4}{16} = \frac{10}{16} = \frac{5}{8} = 0.625$$

↓
62.5%

12. A spinner is numbered from 1 through 10 with each number equally likely to occur. What is the probability of obtaining a number less than 2 in a single spin? 1 2 3 4 5 6 7 8 9 10

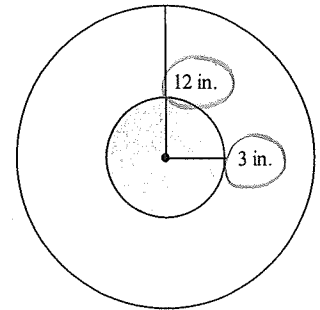
$$P(<2) = \frac{1}{10} = 0.1 \rightarrow 10\%$$

13. If a dart hits the target at random, what is the probability that it will land in the shaded region? (Remember: Area of a circle = πr^2)

$$\begin{aligned} \text{Area (shaded)} &= \pi(3)^2 = 9\pi \\ \text{Area (total)} &= \pi(12)^2 = 144\pi \end{aligned}$$

$$P(\text{shaded}) = \frac{9\pi}{144\pi} = \frac{1}{16} = 0.0625$$

↓
6.25%



Drawing not to scale

Lesson 11.8 – Binomial Theorem

Use the Binomial Theorem to find the binomial expansion of the expression.

14. $(a+b)^6$ 1 6 15 20 15 6 1

$$\begin{aligned} &1a^6b^0 + 6a^5b^1 + 15a^4b^2 + 20a^3b^3 + 15a^2b^4 + 6a^1b^5 + 1a^0b^6 \\ &a^6 + 6a^5b + 15a^4b^2 + 20a^3b^3 + 15a^2b^4 + 6ab^5 + b^6 \end{aligned}$$

Simplified answer: _____

$$4c^3 \cdot 3^1$$

15. $(c-3)^4$ 1 4 6 4 1

$$\begin{aligned} &1c^4(3)^0 - 4c^3(3)^1 + 6c^2(3)^2 - 4c^1(3)^3 + 1c^0(3)^4 \\ &c^4 - 12c^3 + 54c^2 - 108c + 81 \end{aligned}$$

$$4 \cdot c^3 \cdot 3$$

$$12c^3$$

Simplified answer: _____