

Simplify. Write any complex number solutions in **standard form**.

1. $(-3+7i)-(9+12i)$

+1 Standard form

1. $-12-5i$ **2**

2. $(-3-2i)(5-3i)$
 $-15+9i-10i+6i^2$

2. $-21-i$ **2**

3. $(8-\sqrt{-27})+(9+\sqrt{-48})$
 $(8-3i\sqrt{3})+(9+4i\sqrt{3})$

*6 8
2 3 2 2 2*

3. $17+i\sqrt{3}$ **2**

4. $\sqrt{-32}(\sqrt{6}-\sqrt{-3})$
 $4i\sqrt{2}(\sqrt{6}-\sqrt{3}i)$

*2 2 2 2 2
8i\sqrt{3} - 4i^2\sqrt{6}*

4. $4\sqrt{6}+8i\sqrt{3}$ **2**

5. $\sqrt{-49}+\sqrt{12}$
 $7i+2\sqrt{3}$

5. $2\sqrt{3}+7i$ **2**

6. $-5i(7-3i)$
 $-35i+15i^2$

6. $-15-35i$ **2**

7. $\frac{-\sqrt{-64}}{\sqrt{-4}} = \frac{-8i}{-2i}$

7. -4 **2**

8. $\frac{(5+2i)(3-4i)}{(3+4i)(3-4i)} = \frac{15-20i+6i-8i^2}{9-16i^2}$

8. $\frac{23-14i}{25}$ **3**

9. $\frac{1}{2+i} + \frac{3+i}{2+3i}$
 $\frac{1(2+3i)}{(2+i)(2+3i)} + \frac{(3+i)(2+i)}{(2+i)(2+3i)} = \frac{2+3i+6+5i+i^2}{4+8i+3i^2} = \frac{7+8i}{1+8i}$

(7+8i)(1-8i) = 7-56i+8i+64 *unrationalized*

9. $\frac{7+8i}{1+8i}$ **4**

10. i^{33} $(i^2)^{16} i$
 $(-1)^{16}$

10. i **2**

11. Find x and y: $7x-5yi=-28+25i$

11. $x=-4$ **2**
 $y=-5$

For #12-14, solve the equations, finding all real and imaginary solutions. Be sure to simplify all answers.

12. $5x^2 + 2x + 1 = 0$
 $5x^2 + 1 = -2x$

$$\frac{-2 \pm \sqrt{4 - 4(5)(1)}}{10}$$

$$\frac{-2 \pm \sqrt{-16}}{10} = \frac{-2 \pm 4i}{10}$$

12. $\frac{-1 \pm 2i}{5}$ +3

13. $x^4 - 81 = 0$
 $(x^2 - 9)(x^2 + 9)$

(11)

13. $\pm 3, \pm 3i$ +4

14. $3x^4 + 81x = 0$

$$3x(x^3 + 27)$$

$$3x(x+3)(x^2 - 3x + 9)$$

$$\frac{3 \pm \sqrt{9 - 4(1)(9)}}{2}$$

$$\frac{3 \pm \sqrt{-27}}{2}$$

14. $0, -3, \frac{3 \pm 3i\sqrt{3}}{2}$ 4

For #15-18, find a polynomial with real coefficients that satisfy the given conditions. Leave your answer in factored form without any imaginary numbers.

15. degree 5: zeros include 4 (multiplicity 3), and $3 - 4i$

$$(x-4)^3 (x - (3-4i))(x - (3+4i))$$

$$(x-3)^2 + 16$$

$$x^2 - 6x + 9 + 16$$

15. $(x-4)^3 (x^2 - 6x + 25)$ 5

16. degree 2: zeros include $1 - 2i$; $f(2) = 4$

$$(x - (1-2i))(x - (1+2i))$$

$$(x-1)^2 + 4$$

$$x^2 - 2x + 1 + 4$$

$$y = a(x^2 - 2x + 5)$$

$$4 = a(5)$$

16. $\frac{4}{5}(x^2 - 2x + 5)$ 4

17. Find **all** the zeros of the polynomial

$$g(x) = x^4 - 2x^3 + 5x^2 - 8x + 4, \text{ given } 1 \text{ is a zero of multiplicity of } 2.$$

$$\begin{array}{r|rrrrr} 1 & 1 & -2 & 5 & -8 & 4 \\ & & 1 & -1 & 4 & -4 \\ \hline & 1 & -1 & 4 & -4 & 0 \end{array}$$

$$\begin{array}{r|rrrr} 1 & 1 & -1 & 4 & -4 \\ & & 1 & 0 & -4 \\ \hline & 1 & 0 & 4 & 0 \end{array}$$

$$x^2 + 4 = 0$$

17. $1, \pm 2i$ 3

18. Find **all** the zeros of the polynomial

$$g(x) = 2x^4 - x^3 + 7x^2 - 4x - 4, \text{ given that } 2i \text{ is a zero.}$$

$$(x-2i)(x+2i)$$

$$x^2 + 4$$

$$\begin{array}{r} x^2 + 4 \overline{) 2x^4 - x^3 + 7x^2 - 4x - 4} \\ \underline{2x^4 + 8x^2} \\ -x^3 - x^2 - 4x - 4 \end{array}$$

$$\begin{array}{r} -x^3 - x^2 - 4x - 4 \\ \underline{-x^3 - 4x} \\ -x^2 - 4x - 4 \end{array}$$

(28)

18. $\pm 2i, -\frac{1}{2}, 1$ 4

$$-x^2 - 4$$

$$(2x^2 - x - 1)$$

$$(2x+1)(x-1)$$

Simplify. Write any complex number solutions in **standard form**.

1. $(-3+7i)-(9+12i)$

1. _____

2. $(-3-2i)(5-3i)$

2. _____

3. $(8-\sqrt{-27})+(9+\sqrt{-48})$

3. _____

4. $\sqrt{-32}(\sqrt{6}-\sqrt{-3})$

4. _____

5. $\sqrt{-49}+\sqrt{12}$

5. _____

6. $-5i(7-3i)$

6. _____

7. $\frac{-\sqrt{-64}}{\sqrt{-4}}$

7. _____

8. $\frac{5+2i}{3+4i}$

8. _____

9. $\frac{1}{2+i} + \frac{3+i}{2+3i}$

9. _____

10. i^{33}

10. _____

11. Find x and y : $7x-5yi=-28+25i$

11. _____

For #12-14, solve the equations, finding all real and imaginary solutions. Be sure to simplify all answers.

12. $5x^2 + 1 = -2x$

12. _____

13. $x^4 - 81 = 0$

13. _____

14. $3x^4 + 81x = 0$

14. _____

For #15-18, find a polynomial with real coefficients that satisfy the given conditions. Leave your answer in factored form without any imaginary numbers.

15. degree 5: zeros include 4 (multiplicity 3), and $3 - 4i$

15. _____

16. degree 2: zeros include $1 - 2i$; $f(2) = 4$

16. _____

17. Find **all** the zeros of the polynomial

$g(x) = x^4 - 2x^3 + 5x^2 - 8x + 4$, given 1 is a zero of multiplicity of 2.

17. _____

18. Find **all** the zeros of the polynomial

$g(x) = 2x^4 - x^3 + 7x^2 - 4x - 4$, given that $2i$ is a zero.

18. _____