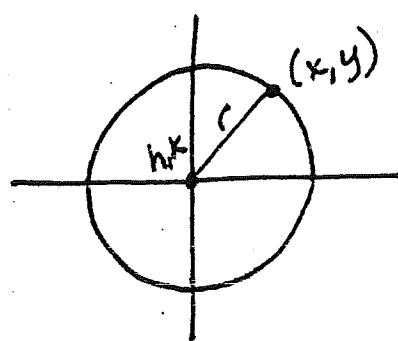


Circles

Circle = set of all points on a plane that are equidistant from a fixed point.

The fixed point is called the center  $(h, k)$ .

The distance is called the radius.



use the distance formula

$$r = \sqrt{(x-h)^2 + (y-k)^2}$$

$$r^2 = (x-h)^2 + (y-k)^2$$

[if center is  $(0,0)$ ]

$$r^2 = x^2 + y^2$$

square  
both  
sides

example:

$$(x-3)^2 + (y+2)^2 = 16$$

← Standard Form

$$(x-h)^2 + (y-k)^2 = r^2$$

$$\text{center: } (3, -2)$$

$$\text{radius: } 4$$

$$(x-3)^2 + (y+2)^2 = 16$$

Convert to General Form

↓

$$x^2 - 6x + 9 + y^2 + 4y + 4 = 16$$

$$x^2 - 6x + y^2 + 4y + 13 = 16$$

$$-13 -1$$

$$x^2 + y^2 - 6x + 4y = 3$$

$$x^2 + y^2 - 6x + 4y - 3 = 0$$

General Form

example:

$$x^2 + (y-5)^2 = 25$$

$$\text{center: } (0, 5)$$

$$\text{radius: } 5$$

$$-\frac{6}{2} = (-3)^2$$

$$\frac{4}{2} \neq (2)^2$$

How do you take an equation in general form and convert it to standard form so that you can graph it?

example:  $x^2 + y^2 - 6x + 4y - 3 = 0$  General form

$$x^2 - 6x + \underline{\underline{9}} + y^2 + 4y + \underline{\underline{4}} = \underline{\underline{3}} + \underline{\underline{9}} + \underline{\underline{4}}$$

↓  
Standard form

$$(x-3)^2 + (y+2)^2 = 16$$

Center:  $(3, -2)$   $r=4$

example:  $\frac{3x^2}{3} + \frac{3y^2}{3} + \frac{12x}{3} + \frac{12}{3} = \frac{18y}{3}$

$$x^2 + y^2 + 4x + 4 = 6y$$

$$x^2 + 4x + \underline{\underline{4}} + y^2 - 6y + \underline{\underline{9}} = -4 + \underline{\underline{4}} + 9$$
$$(x+2)^2 + (y-3)^2 = 9$$

Center  $(-2, 3)$   $r=3$

example: Find the equation of a circle w/ center  $(-1, -3)$  passing through  $(-4, -2)$

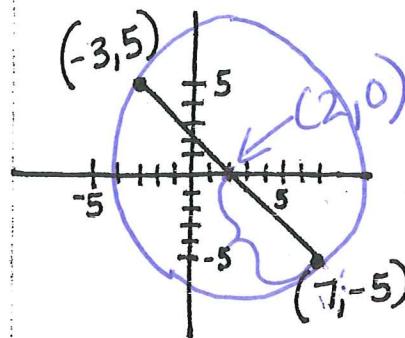
$$(x-h)^2 + (y-k)^2 = r^2$$

$$(-4 + \underline{-1})^2 + (-2 + \underline{-3})^2 = r^2$$

$$9 + 1 = r^2$$
$$10 = r^2$$

$$(x+1)^2 + (y+3)^2 = 10$$

example: Find the equation with endpoints of a diameter  $(-3, 5)$  and  $(7, -5)$



$$r = 5\sqrt{2}$$

$$r^2 = 50$$

$$d = \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$$

$$d = \sqrt{(7 - -3)^2 + (-5 - 5)^2}$$

$$d = \sqrt{(10)^2 + (-10)^2}$$

$$d = \sqrt{100 + 100}$$

$$d = \sqrt{200}$$

$$d = \frac{10\sqrt{2}}{2}$$

The radius is  $\frac{1}{2}$  of  $10\sqrt{2}$

$$r = 5\sqrt{2}$$

Now find the midpoint because this is the center point

$$\text{Midpoint} : \left( \frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$$

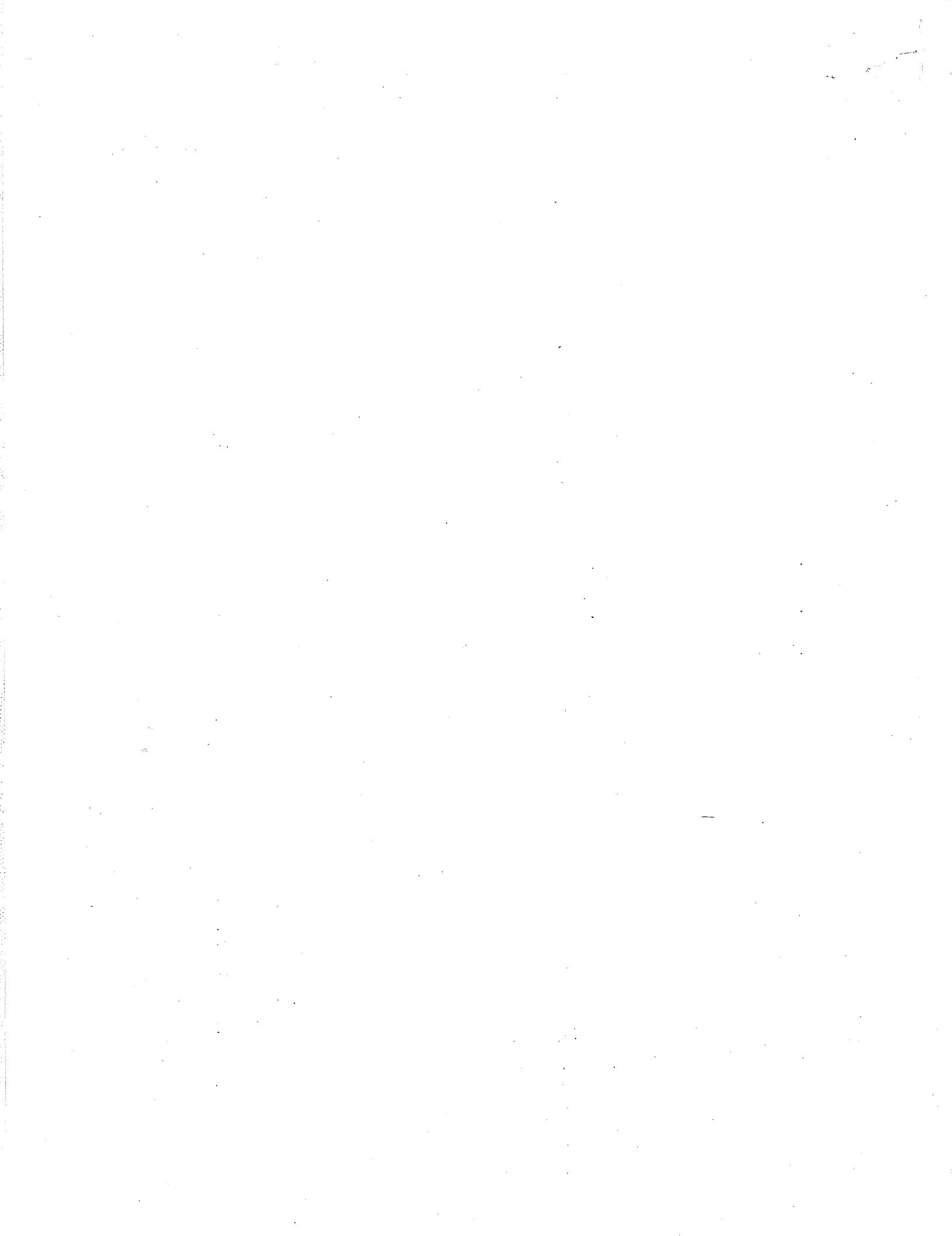
$$\left( \frac{-3+7}{2}, \frac{5+(-5)}{2} \right)$$

$$\left( \frac{4}{2}, \frac{0}{2} \right)$$

$$\text{center} : (2, 0)$$

$$(x-2)^2 + y^2 = (5\sqrt{2})^2$$

$$(x-2)^2 + y^2 = 50$$



## Pre Calc Circles

Name \_\_\_\_\_

In Exercises 11–14, find the equation of the circle with given center and radius  $r$ .

11.  $(-3, 4); r = 2$

12.  $(-2, -1); r = 3$

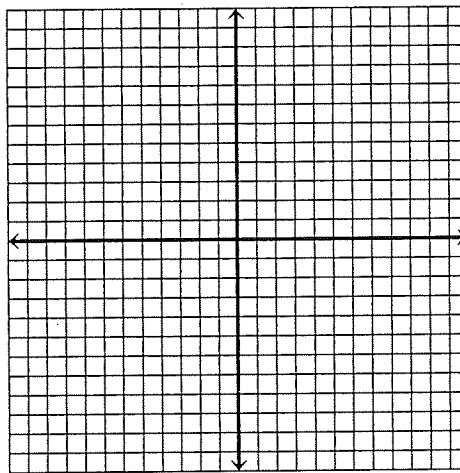
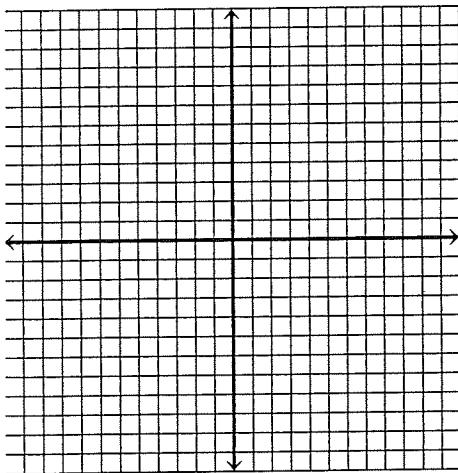
13.  $(0, 0); r = \sqrt{2}$

14.  $(5, -2); r = 1$

In Exercises 15–18, sketch the graph of the equation.

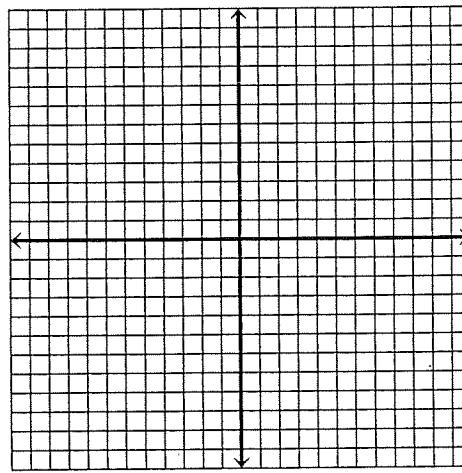
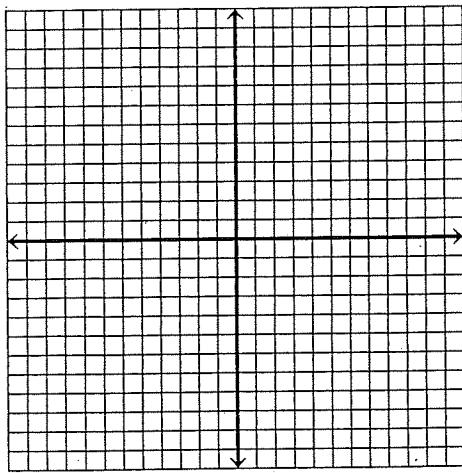
15.  $(x - 2)^2 + (y - 4)^2 = 1$

16.  $(x + 1)^2 + (y - 3)^2 = 9$



17.  $(x - 5)^2 + (y + 2)^2 = 5$

18.  $(x + 6)^2 + y^2 = 4$



In Exercises 19–24, find the center and radius of the circle whose equation is given.

19.  $x^2 + y^2 + 8x - 6y - 15 = 0$

21.  $x^2 + y^2 + 6x - 4y - 15 = 0$

23.  $x^2 + y^2 + 25x + 10y = -12$

In Exercises 29–36, find the equation of the circle.

29. Center (2, 2); passes through the origin.

31. Center (1, 2); intersects x-axis at -1 and 3.

33. Center (-5, 4); tangent (touching at one point) to the x-axis.