

3.3 Quadratic Functions Day 2 Notes and Homework

In this section, you will learn how to convert each quadratic function into the various forms.

How do you go from X-Intercept Form (IF) or Transformation Form (TF) to Polynomial Form:

$$IF \rightarrow PF$$

A. $f(x) = -2(x-4)(x+2)$
 $f(x) = -2(x^2 - 2x - 8)$
 $f(x) = -2x^2 + 4x + 16$

Set $x=0$

$$TF \rightarrow PF$$

B. $f(x) = 3(x-2)^2 - 47$
 $3(x^2 - 4x + 4) - 47$
 $3x^2 - 12x + 12 - 47$
 $f(x) = 3x^2 - 12x - 35$

1. $f(x) = 3(x-2)(x+1)$

2. $f(x) = -2(x-5)(x-2)$

3. $f(x) = -2(x+3)^2 - 4$

How do you go from Polynomial Form (PF) to Transformation Form (TF): $PF \rightarrow TF$

2 Ways:

$$y = a(x-h)^2 + k$$

$(4, -20)$

A. Find the Vertex

$$f(x) = 2x^2 - 16x + 12$$

$$x = -\frac{b}{2a} = \frac{16}{2(2)} = 4$$

$$y = 2(4)^2 - 16(4) + 12 = -20$$

$$y = 2(x-4)^2 - 20$$

B. Complete the square

$$f(x) = 2x^2 - 12x + 14$$

$$\begin{aligned} f(x) &= 2x^2 - 12x + 14 \\ &= 2(x^2 - 6x + 9) + 14 - 18 \\ f(x) &= 2(x-3)^2 - 4 \end{aligned}$$

4. $f(x) = 3x^2 - 12x + 10$

5. $f(x) = -6x^2 - 12x - 1$

6. $f(x) = x^2 - 6x - 3$

How to convert from Polynomial Form (PF) to X Intercept Form (IF): $PF \rightarrow IF$

quad
comp.

A. $f(x) = x^2 + 4x - 5$

$$f(x) = (x+5)(x-1)$$

B. $f(x) = 3x^2 - 14x - 5$

$$= (3x+1)(x-5)$$

$x = -\frac{1}{3}$

$x = 5$

$$f(x) = 3\left(x + \frac{1}{3}\right)(x-5)$$

C. $f(x) = x^2 - 8x - 3$

$x^2 - 8x - 3 = 0$

$$\begin{aligned} x^2 - 8x + 16 &= 3 + 16 \\ (x-4)^2 &= 19 \\ x &= 4 \pm \sqrt{19} \end{aligned}$$

$$f(x) = (x - (4 + \sqrt{19}))(x - (4 - \sqrt{19}))$$

7. $f(x) = x^2 + 2x - 5$

8. $f(x) = x^2 - 4x + 6$

9. $f(x) = 2x^2 - x - 3$

How to go from X intercept form (IF) to Transformation Form (TF): $IF \rightarrow TF$

A. $f(x) = -2(x-4)(x+2)$

$$\begin{array}{l|l} x=1 & -2(1-4)(1+2) \\ \uparrow & -2(-3)(2)=18 \\ & (1, 18) \\ \hline y & -2(x-1)^2+18 \end{array}$$

3 ways to do this one:

$$-2(x^2 - 2x - 8)$$

$$y = -2x^2 + 4x + 16$$

$$x = \frac{-b}{2a} = \frac{-4}{-4} = 1$$

$y = 18$

$$y = -2(x-1)^2 + 18$$

$$y = -2x^2 + 4x + 16$$

$$y = -2x^2 + 4x + 16$$

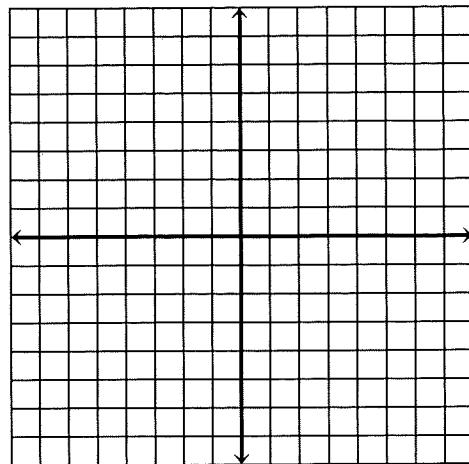
$$-2(x^2 - 2x + 1) + 16 + 2$$

$$y = -2(x-1)^2 + 18$$

10. $f(x) = 3(x+1)(x-5)$

11. $f(x) = -4(x-6)(x+2)$

12. $f(x) = -6(x-2)^2 - 5$



a. _____
Polynomial form

X intercept form

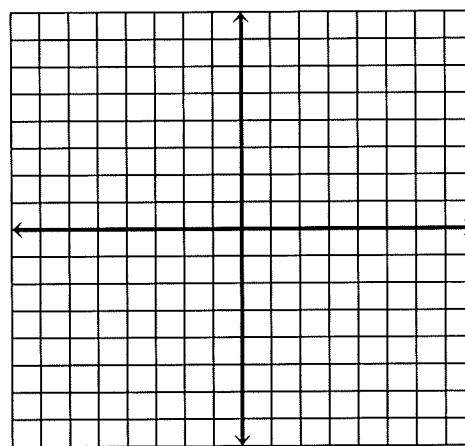
b. up or down: _____

c. axis of symmetry : _____

d.x-int: _____

y-int: _____

13. $f(x) = 4(x-2)(x+1)$



a. _____
Polynomial form

Transformation form

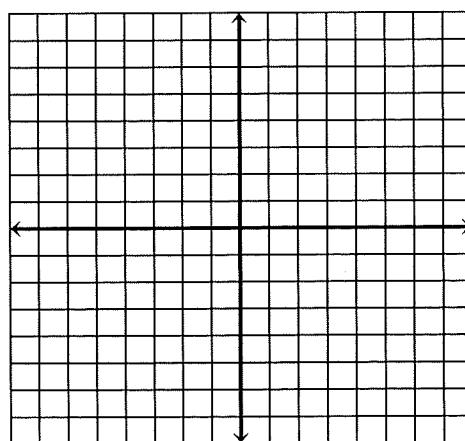
b. up or down: _____

c. axis of symmetry : _____

d.x-int: _____

y-int: _____

14. $f(x) = 3x^2 + 24x + 45$



a. _____
X intercept form

Transformation form

b. up or down: _____

c. axis of symmetry : _____

d.x-int: _____

y-int: _____

